

## STATEMENT OF WORK

16 April 2004

This request is for a non-personal services contract for an individual scientist to perform research in the area of mathematically modeling the electromagnetic sensing of chiral and achiral materials and teach mathematics courses in direct support of the AFIT/ENC mission. The contractor will conduct advanced research in the area of electromagnetics, provide classroom instruction in graduate mathematics courses and review of undergraduate mathematics courses, and provide consultations with faculty and students. The contractor's work will be performed at the Air Force Institute of Technology, Graduate School of Engineering and Management, Department of Mathematics and Statistics. The contractor will do the following research and teaching:

RESEARCH: (28 Jun 04 – 24 June 05): Investigate ways of incorporating advanced topics in mathematics into the modeling of the electromagnetic sensing of chiral and achiral materials with the goal of improving existing techniques for detecting biological weapons. In particular, he/she will find ways in which areas such as complex analysis, generalized Fourier transforms, and wavelets can be brought to bear on fundamental problems of modeling such materials. The contractor will also investigate ways in which these improved techniques can be used to solve outstanding problems of particular interest to the Air Force and Department of Defense. The contractor will give quarterly oral reports and a final written report on his/her findings to the faculty of the Department of Mathematics and Statistics. The quality of the research conducted is expected to be such that technical peers will judge the final results to be original and publishable in appropriate archival, refereed, professional journals.

TEACHING: The contractor will prepare and teach the following courses:

MATH 509, Mathematical Methods in the Physical Sciences

Summer Quarter, 28 Jun 04 -10 Sep 04

One section. 4 hours of lecture per week per section. 10 weeks of class and a final exam

Mathematics Review

2<sup>nd</sup> Half of Fall Short Term, 20 Sep 04 – 1 Oct 04

One section. 10 hours of lecture per week per section. Two (2) weeks of class.

MATH 511, Methods of Applied Mathematics I

Fall Quarter, 4 Oct 04 – 17 Dec 04

Two sections. 4 hours of lecture per week per section. 10 weeks of class and a final exam

MATH 508, Applied Numerical Methods

Winter Quarter, 3 Jan 05 – 17 Mar 05

One section. 4 hours of lecture per week per section. 10 weeks of class and a final exam

MATH 674, Numerical Analysis I

Spring Quarter, 28 Mar 05 – 10 Jun 05

One section. 4 hours of lecture per week per section. 10 weeks of class and a final exam

Mathematics Review

2<sup>nd</sup> Half of Summer Short Term, 13 Jun 05 – 24 Jun 05.

One section. 10 hours of lecture per week per section. Two (2) weeks of class.

**Services Required:** Services include preparation and presentation of a quarterly oral report and a final written report on the research findings; for classes taught, services include preparing class lectures, course outline, handout materials, grading papers and problem assignments, quizzes (if needed), midterm and final exams, and five hours of scheduled office consultation per week. For classes taught, quizzes, exams, problems, and class participation will be evaluated and final grades with justification will be submitted to the Head, Department of Mathematics and Statistics, by suspense date (to be determined). Classes will be taught at times as scheduled by the AFIT Registrar (AFIT/RR), or as arranged by the instructor with students with the approval of the Head, Department of Mathematics and Statistics.

**Mathematics Review** is a noncredit review of the fundamentals of various elementary mathematics courses in order to prepare the student for graduate study. Topics from elementary calculus, linear algebra, and differential equations will be covered depending on the needs of the students.

**MATH 509, Mathematical Methods in the Physical Sciences**, covers basic topics in linear algebra and the calculus of several variables. Topics in linear algebra include matrix algebra, solutions of systems of linear equations, real vector spaces, and linear transformations between real vector spaces. Topics from several variable calculus include partial differentiation, directional derivatives, functional transformations and Jacobians, maxima and minima, and integration in two and three variables.

**MATH 511, Methods of Applied Mathematics I**, is an introductory graduate level course in the methods of applied mathematics. Topics covered include differential and integral calculus of functions of several variables, vector differential calculus, directional derivatives, gradient, divergence and curl, line and surface integrals, Green's theorem, divergence theorem and Stokes' theorem, Fourier series expansions, partial differential equations of applied science, complex numbers, and analytic functions of a complex variable.

**MATH 508, Applied Numerical Methods**, is designed primarily to provide digital computer-oriented methods for determining roots of equations, solutions of systems of equations, approximation of functions, values of definite integrals, solutions of ordinary and partial differential equations, and matrix eigenvalue problems.

**MATH 674, Numerical Analysis I**, is designed primarily to develop ways to rigorously analyze numerical methods such as those used to find roots of nonlinear equations, interpolation and approximation of functions, techniques for numerical integration and differentiation, techniques for solving ordinary differential equations. Developing error estimates and convergence analyses for each topic will be included.

#### **Job Tasks Summary:**

**RESEARCH:** The contractor will incorporate advanced topics in mathematics into the modeling of the electromagnetic sensing of chiral and achiral materials with the goal of improving existing modeling techniques and will investigate ways in which these improvements can be used to solve problems of particular interest to the Air Force and Department of Defense. This will require the contractor to find the appropriate problems and demonstrate the applicability and effectiveness of the new techniques. The contractor will give quarterly oral reports and a final written report on his/her findings to the faculty of the Department of Mathematics and Statistics.

TOTAL RESEARCH HOURS	1000 hours
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TEACHING:

MATH 509 (Summer Quarter)

Lectures (1 section at 4 hours/week/section for 10 weeks)	40 hours.
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Lecture preparation, testing, and grading	120 hours
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Office hours [5 hours/week for 10 weeks]	<u>50 hours</u>
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TOTAL HOURS:	210 hours
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Mathematics Review (2<sup>nd</sup> Half of Fall Short Term)

Lectures (1 section at 10 hours/week/section for 2 weeks)	20 hours
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Lecture preparation	40 hours
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Office hours (5 hours/week for 2 weeks)	<u>10 hours</u>
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TOTAL HOURS	70 hours
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MATH 511 (Fall Quarter)

Lectures (2 sections at 4 hours/week/section for 10 weeks)	80 hours
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Lecture preparation, testing, and grading	140 hours
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Office hours [5 hours/week for 10 weeks]	<u>50 hours</u>
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TOTAL HOURS:	270 hours
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MATH 508 (Winter Quarter)

Lectures (1 section at 4 hours/week/section for 10 weeks)	40 hours
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Lecture preparation, testing, and grading	120 hours
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Office hours [5 hours/week for 10 weeks]	<u>50 hours</u>
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TOTAL HOURS:	210 hours
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MATH 674 (Spring Quarter)

Lectures (1 section at 4 hours/week/section for 10 weeks)	40 hours
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Lecture preparation, testing, and grading	120 hours
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Office hours [5 hours/week for 10 weeks]	<u>50 hours</u>
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TOTAL HOURS:	210 hours
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Mathematics Review (2<sup>nd</sup> Half of Summer Short Term)

Lectures (1 section at 10 hours/week/section for 2 weeks)	20 hours
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Lecture preparation	40 hours
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Office hours [5 hours/week for 10 weeks]	<u>10 hours</u>
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TOTAL HOURS	70 hours
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TOTAL INSTRUCTIONAL RELATED HOURS:	1040 hours
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GRAND TOTAL HOURS (Research & Instruction)	2040 hours
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